



Disordered pyrochlore CsMgInF₆ at high pressures

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ABSTRACT

High pressure behaviour of disordered pyrochlore CsMgInF₆ (*Pnma*, *Z* = 4) has been studied with powder and single-crystal X-ray diffraction to 8.0 and 6.94 GPa, respectively, in diamond anvil cells at room temperature. The material is structurally stable to at least 8.0 GPa with no ordering of the In³⁺ and Mg²⁺ cations. The *P*–*V* data are fitted by a Birch–Murnaghan equation of state with the zero-pressure bulk modulus *B*₀ = 33.4(3) GPa and the unit-cell volume at ambient pressure *V*₀ = 603.2(4) Å³ for the first pressure derivative of the bulk modulus *B*' = 4.00. The major contribution to the bulk compressibility arises from the changes in the coordination sphere around the Cs atoms. The effect of hydrostatic pressure on the crystal structure of CsMgInF₆ is comparable to the effect of chemical pressure induced by the incorporation of ions of different sizes into the *A* and *B* sites in defect AB²⁺B'³⁺F₆ pyrochlores.

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1. Introduction

Ideal pyrochlore (*Fd* $\bar{3}m$, *Z* = 8) has a formula A₂B₂X₆X' (A = Na, Rb, Cs, Ca, Sr, Mg, etc.; B = Nb, Ta, Ti, Fe, etc.; X and X' = O, F, or OH). The *A* cations are coordinated by eight anions, while the *B* cations are in an octahedral coordination. When a large cation, like Cs¹⁺, Rb¹⁺, K¹⁺, or NH₄¹⁺ is incorporated into one of the *A* sites (the other remaining empty) in fluoride pyrochlore, a defect structure with a formula AB²⁺B'³⁺F₆ is obtained. The coordination numbers of the Cs¹⁺ and Rb¹⁺ cations vary from 12+6 to 18.¹ There is only one symmetrically independent *B* site in the ideal cubic structure so that the two B²⁺ and B'³⁺ cations are perfectly disordered. Ordering of these cations leads to symmetry lowering and the ordered compounds crystallize in space groups which are in a group–subgroup relation to *Fd* $\bar{3}m$ [1] (Fig. 1). CsMgInF₆ is a remarkable representative of the AB²⁺B'³⁺F₆ family [2] as no ordering of the Mg²⁺ and In³⁺ cations occurs on the *B* site, although its symmetry is orthorhombic (*Pnma*, *Z* = 4). The compound is multiply twinned at ambient conditions, the twinning elements being a combination of the three- and four-fold rotation axes of the archetype cubic lattice.

In our previous work on NaCdZn₂F₇ and NaCaMg₂F₇ (*Fd* $\bar{3}m$, *Z* = 8), in which the Na¹⁺/Cd²⁺ and Na¹⁺/Ca²⁺ cations are perfectly

disordered on the *A* site, we demonstrated that they are structurally stable at least to 9.0 and 6.5 GPa, respectively, with no indication either for ordering or for structural transformations [3]. In this work, we continue our interest in disordered fluoride pyrochlores and investigate the crystal structure of CsMgInF₆ (*Pnma*, *Z* = 4) at different pressures and room temperature. Our main goal is to examine (dis)ordering of the Mg²⁺ and In³⁺ cations and structural distortions using X-ray powder and single-crystal diffraction.

2. Experimental

Single-crystal and powder samples of CsMgInF₆ investigated here have already been used in Ref. [2].

The ruby luminescence method [4] was used for pressure calibration and a 4:1 mixture of methanol and ethanol was used as a pressure medium during the powder and single-crystal measurements. The error in pressure determination is estimated to be 0.02 GPa.

High-pressure room-temperature X-ray powder diffraction studies were performed at the beamline D3 in HASYLAB (Hamburg, Germany). Finely ground samples were loaded into a DXR-6 (Diacell) diamond anvil cell for angle-dispersive powder X-ray diffraction measurements to 8.0 GPa with monochromatic radiation at 0.4 Å. The collimator slits were set to 50 × 50 μm. The diamond cell was optically aligned on the four-circle diffractometer. The data were collected on a marCCD165 detector. The images were integrated with the program FIT2D [5] to yield intensity versus 2θ diagrams. A fluorite powder was added as an

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¹ Although the *A* atoms are generally surrounded by 18 fluorine atoms, only in some of the defect pyrochlores all the fluorines are the *A* nearest neighbours. In several other compounds, a part of the fluorines is closer to the *A* atoms, leading to coordination spheres best described as 12+6, 14+4, 15+3, or 16+2 [1,2].

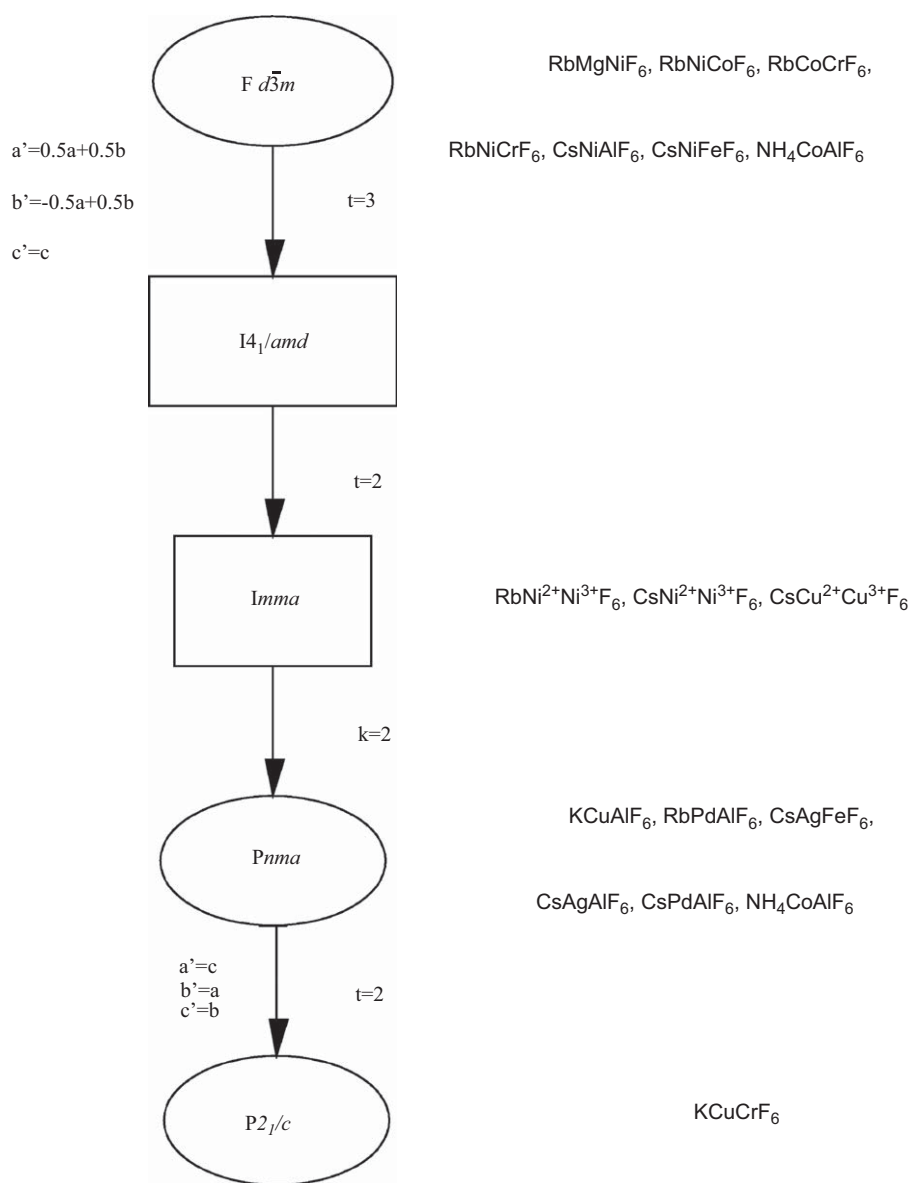


Fig. 1. Group-subgroup relationship for the $AB^2B^3F_6$ pyrochlores with a few relevant examples included in Ref. [1].

internal standard for the 2θ calibration at each pressure through the CaF_2 equation of state [6].

Single-crystal intensities were measured from a crystal with approximate dimensions $0.07 \times 0.04 \times 0.06$ mm at room temperature to 6.94 GPa in a diamond anvil cell of the Boehler-Almax type using a STOE diffractometer IPDS-2 T (MoK α). A 250 μ m hole was drilled into a stainless steel gasket preindented to a thickness of about 80 μ m. The intensities were indexed and integrated using the STOE software [7]. Shaded areas of the images by the diamond anvil cell were masked prior to integration. The intensities were integrated simultaneously with three orientation matrices, corresponding to the crystal of CsMgInF₆ and to the two diamonds of the cell. The corrections for the effect of absorption by the diamond anvils and the crystal were made using the program Absorb [8] and the STOE software [7], respectively. Structural refinements were carried out with the program JANA2006 [9].²

² Further details of the crystallographic investigations can be obtained from the Fachinformationszentrum Karlsruhe, D-76344 Eggenstein-Leopoldshafen, Germany, on quoting the depository number CSD 420660.

3. Results and discussion

The lattice parameters and unit-cell volume of CsMgInF₆ ($Pnma$, $Z = 4$) at atmospheric pressure are $a = 7.5285(1)$ Å, $b = 7.5285(1)$ Å, $c = 10.6459(1)$ Å, and $V = 603.39(1)$ Å³, respectively [2]. This metrics is not only tetragonal, but it also reflects the cubic lattice of the underlying ideal pyrochlore structure, $a = b \approx c/\sqrt{2}$. As a consequence, splitting of reflections indicating the symmetry reduction in X-ray powder diffraction diagrams is difficult to detect at atmospheric pressure. In addition, the reflections violating the extinction rules for the cubic face-centered lattice (or the tetragonal/orthorhombic body-centered lattice) and thus providing the conclusive indication for the symmetry lowering are extremely weak. However, our powder X-ray data collected at high pressures clearly demonstrate splitting of reflections due to either an anisotropic compressibility of the material or a pressure-induced phase transition (Fig. 2). All the changes in the patterns are reversible on decompression, although the reflections are slightly more broadened and thus worse resolved than before the compression.

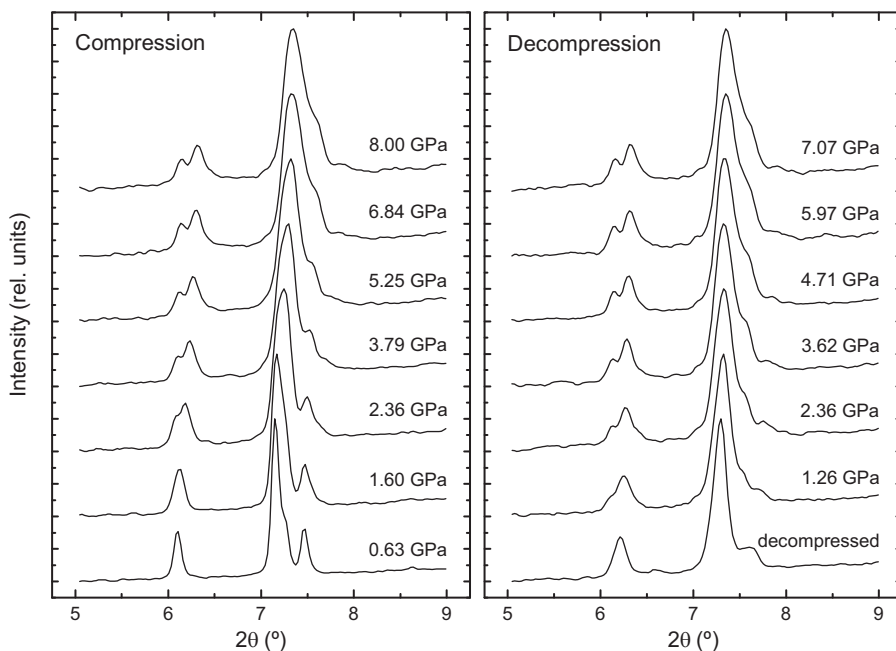


Fig. 2. X-ray powder diffraction diagrams in the 2θ range from 5° to 9° as a function of pressure.

Table 1

Pressure dependence of lattice parameters and unit-cell volume.

Pressure (GPa)	a (Å)	b (Å)	c (Å)	V (Å ³)
0.0001	7.5285(1)	7.5285(1)	10.6459(1)	603.4
1.08	7.435(3)	7.489(3)	10.491(4)	584.1
2.32	7.332(3)	7.467(4)	10.368(4)	567.6
3.39	7.240(4)	7.432(4)	10.289(4)	553.6
4.53	7.165(4)	7.411(4)	10.202(5)	541.7
5.33	7.088(5)	7.389(5)	10.174(6)	532.8
6.04	7.021(4)	7.362(4)	10.162(5)	525.3
6.94	6.965(4)	7.335(5)	10.134(6)	517.7

Estimated standard deviations are in brackets.

More information on the high-pressure behaviour of CsMgInF₆ was obtained from single-crystal X-ray diffraction. An inspection of reciprocal space sections reconstructed from data sets at different pressures also revealed splitting of reflections. Indexing always yielded a primitive orthorhombic lattice. Although reflections violating the body-centered lattice are very weak, a small number of them could be reliably observed. Taking into account the twinning model described in [2], the data are in accordance with space group $Pnma$ at all pressures. This observation indicates that CsMgInF₆ does not undergo any structural phase transformation up to at least 6.94 GPa.

The pressure dependence of the lattice parameters and unit-cell volumes obtained from single-crystal X-ray data (Table 1) is presented in Fig. 3. CsMgInF₆ is the most and the least compressible along the a and b axes, respectively. The P – V data could be fitted by a Birch–Murnaghan equation of state³ with the zero-pressure bulk modulus $B_0 = 33.4(3)$ GPa and the unit-cell volume at ambient pressure $V_0 = 603.2(4)$ Å³ for the first pressure derivative of the bulk modulus $B' = 4.00$.

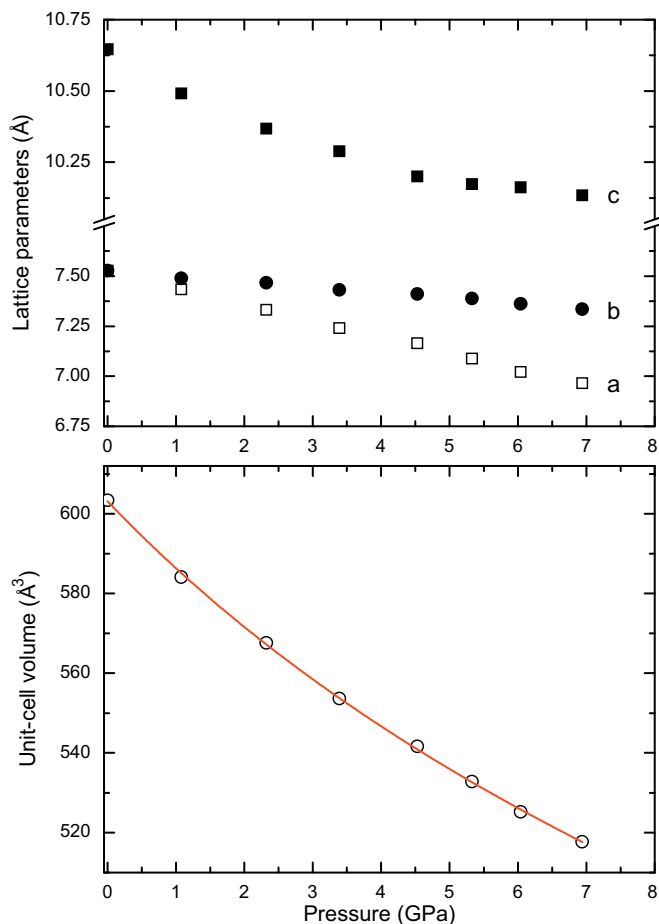


Fig. 3. Pressure dependence of the lattice parameters and unit-cell volume. The solid line represents the fit to the compressibility data using the Birch–Murnaghan equation of state: $V_0 = 603.2(4)$ Å³, $B_0 = 33.4(3)$ GPa, and $B' = 4.00$.

³ Program EoS-Fit V5.2 by Ross Angel, www.crystal.vt.edu/crystal/software.html

Table 2
Experimental data for the measurements at 6.04 GPa (*Pnma*, *Z* = 4).

<i>Crystal data</i>	
<i>a</i> (Å)	7.021(4)
<i>b</i> (Å)	7.362(4)
<i>c</i> (Å)	10.162(5)
<i>V</i> (Å ³)	525.3
ρ (g/cm ³)	4.880
μ (mm ⁻¹)	11.487
<i>Data collection</i>	
No. measured refl.	2731
Range of <i>hkl</i>	$-8 \leq h \leq 7$ $-7 \leq k \leq 8$ $-11 \leq l \leq 11$
No. unique refl.	512
No. observed refl. ^a	119
<i>R</i> (int) _{obs/all} ^b	10.19/15.52
$\sin(\theta)/\lambda$	0.6679
<i>Refinement</i> ^b	
<i>R</i> _{obs}	9.31
<i>wR</i> _{obs}	7.46
<i>GoF</i> _{obs}	1.53
No. parameters	26

^a Criterion for observed reflections is $|F_{\text{obs}}| > 3\sigma$.^b All agreement factors are given in %, weighting scheme $1/[\sigma^2(F_{\text{obs}}) + (0.01F_{\text{obs}})^2]$.**Table 3**
Positional and isotropic thermal displacement parameters (in Å²) at 6.04 GPa (*Pnma*, *Z* = 4).

Atom	W.P.	<i>x</i>	<i>y</i>	<i>z</i>	<i>U</i> _{iso}	Occupancy
Cs	4c	0.4767(13)	0.25	0.3665(7)	0.050(3)	1.0
In1/Mg1	4b	0.0	0.0	0.5	0.052(3)	0.5/0.5
In2/Mg2	4c	0.287(2)	0.25	0.7156(14)	0.051(4)	0.5/0.5
F1	8d	0.305(6)	0.022(5)	0.835(3)	0.078(8)	1.0
F2	8d	0.235(6)	0.425(5)	0.549(4)	0.078(8)	1.0
F3	4c	0.365(8)	0.25	-0.008(5)	0.078(8)	1.0
F4	4c	0.090(7)	0.25	0.827(6)	0.078(8)	1.0

The structural refinement of the data set at 6.04 GPa was performed with the program Jana2006 [9] (Table 2). The starting model in space group *Pnma* (*Z* = 4) was derived from the ideal pyrochlore structure (*Fd3m*, *Z* = 4) using group-subgroup relations for splitting of Wyckoff positions (program WYCKSPLIT [10]).⁴ Initially, the fluorine atoms were fixed at the ideal position derived from the cubic archetype and only the heavy atoms were refined. In subsequent refinement cycles, the symmetry restrictions on the positional parameters of the anionic sublattice were eliminated. The refinement of the occupancy factors of the In and Mg atoms did not indicate any onset of additional ordering. The final refinement (Table 3) included the positional parameters for all atoms, with the occupancies for the two *B* sites maintained at 0.5 In+0.5 Mg. Isotropic thermal parameters were refined for the In/Mg sites. All isotropic displacement parameters for the F atoms were restricted to be equal. The displacement parameter for the Cs atoms, the heaviest in the structure, was refined anisotropically.

Due to the twinning [2], some of the reflections were fully or partially overlapped. They were included in the refinement process allowing for a maximum angular difference of 0.2° for

Table 4
Selected distances (Å) at 6.04 GPa.

<i>Cs</i>	
F1 (2x)	2.84(4)
F1 (2x)	3.25(4)
F1 (2x)	4.17(4)
F2 (2x)	2.82(4)
F2 (2x)	3.25(4)
F2 (2x)	4.29(4)
F2 (2x)	4.77(4)
F3	3.08(5)
F3	3.89(5)
F3	4.53(5)
F3 (2x)	4.57(3)
F4	3.21(6)
F4 (2x)	3.73(1)
<i>In1, Mg1</i>	
F1 (2x)	2.17(4)
F2 (2x)	1.81(4)
F3 (2x)	2.07(2)
<i>In2, Mg2</i>	
F1 (2x)	2.07(4)
F2 (2x)	2.16(4)
F4	1.79(6)
F4	2.17(5)

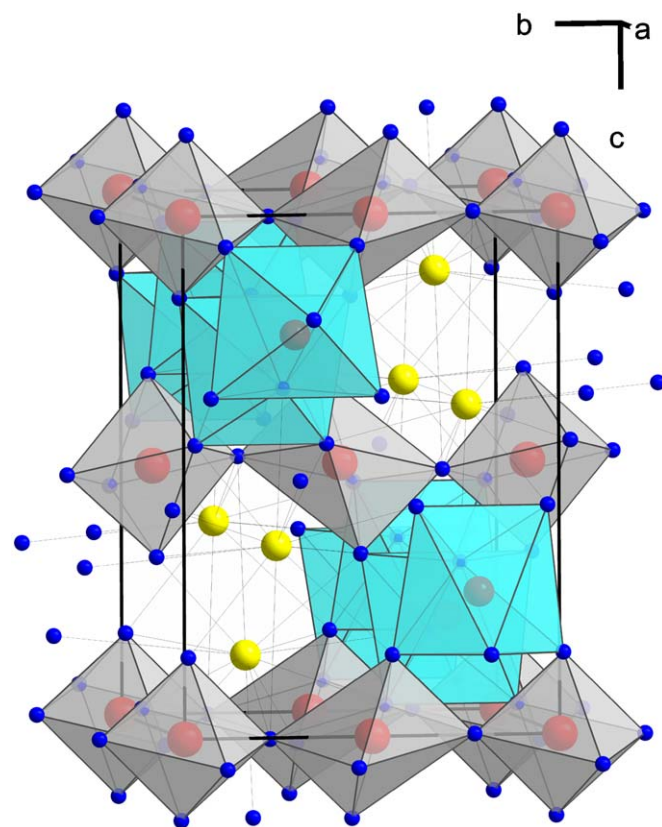


Fig. 4. Crystal structure of CsMgInF₆ (*Pnma*, *Z* = 4) at 6.04 GPa. Yellow, red, and blue symbols represent the Cs, (Mg/In), and F atoms, respectively. Octahedra around the (In1/Mg1) and (In2/Mg2) atoms are drawn grey and cyan, respectively. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

the overlap. The twinning matrices used in the refinements were

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}, \begin{pmatrix} -0.5 & -0.5 & 1 \\ 0.5 & 0.5 & 1 \\ -0.5 & 0.5 & 0 \end{pmatrix}, \begin{pmatrix} -0.5 & 0.5 & -1 \\ -0.5 & 0.5 & 1 \\ 0.5 & 0.5 & 0 \end{pmatrix},$$

⁴ Bilbao Crystallographic Server, www.cryst.ehu.es

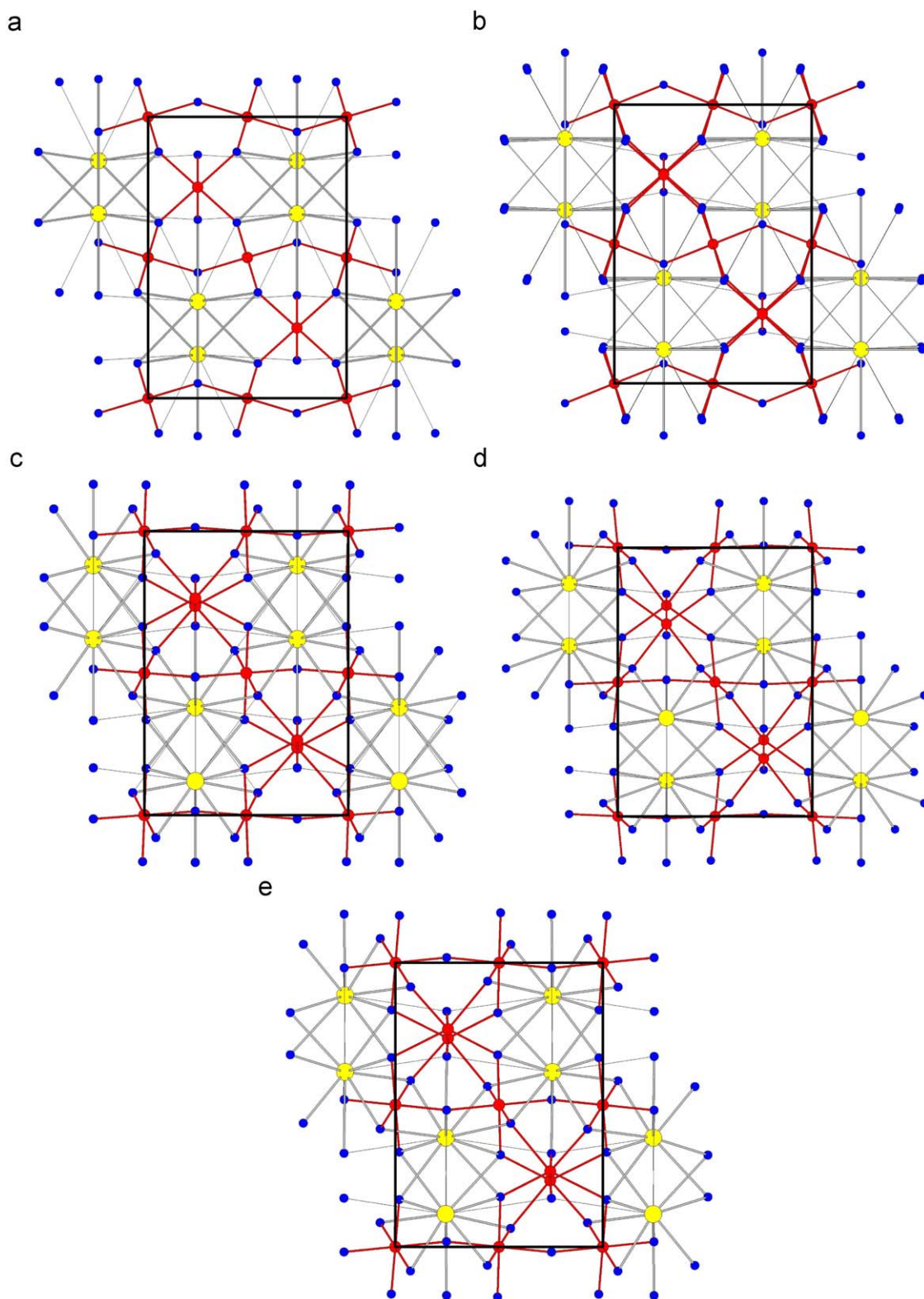


Fig. 5. Cation–fluorine connectivities in the crystal structures of $\text{CsCu}^{2+}\text{Cu}^{3+}\text{F}_6$ ($Imma$, $Z = 4$) (a), CsMgInF_6 ($Pnma$, $Z = 4$) (b), KCuAlF_6 ($Pnma$, $Z = 4$) (c), CsMgInF_6 at 6.04 GPa ($Pnma$, $Z = 4$) (d), and KCuCrF_6 ($P2_1/c$, $Z = 4$) (e). Except for (d), all the other figures depict the connectivities at ambient pressure. The projections for figures (a)–(d) and (e) are (b, c) and (a, c), respectively. Yellow, red, and blue symbols represent the A, B, and F atoms, respectively. The interatomic distances between the B atoms and fluorines below 2.5 Å are drawn red. The interatomic distances between the A atoms and fluorines up to 3.5 Å and from 3.5 to 4 Å are drawn as thick and thin lines, respectively. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

$$\begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}, \begin{pmatrix} 0.5 & -0.5 & 1 \\ -0.5 & 0.5 & 1 \\ -0.5 & -0.5 & 0 \end{pmatrix} \text{ and } \begin{pmatrix} -0.5 & -0.5 & -1 \\ -0.5 & -0.5 & 1 \\ -0.5 & 0.5 & 0 \end{pmatrix}.$$

The refinement of the twin volume fractions lead to a considerable improvement of the overall agreement factors. The fractions are 0.56(2): 0.0: 0.10(2): 0.11(2): 0.17(2): 0.06(2).

The crystal structure of CsMgInF₆ at 6.04 GPa (Table 4 and Fig. 4) is largely distorted in comparison to that at ambient pressure. The major contribution to the bulk compressibility arises from the coordination changes around the Cs atoms. Assuming the limiting distance of 4 Å for the Cs–F interatomic distances, the coordination number of the Cs atoms is 13 (Table 3), while it is 18 at ambient pressure [2]. Four of the distances are below 2.9 Å and are shortened by approximately 13% when compared to the ambient pressure values. The anisotropic compressibilities could well be explained with different pressure-induced changes around the Cs atoms along three crystallographic directions. The largest changes in bonding occur along the *a* axis so that they account for the fact that the *a* linear compressibility is the largest.

Like in all other fluorides, the bulk modulus of CsMgInF₆, $B_0 = 33.4(3)$ GPa, is very small when compared with those of analogous oxides [3,11]. On the other hand, it is also much smaller than those of NaCaMg₂F₇ and NaCdZn₂F₇ pyrochlores, $B_0 \approx 83$ GPa, because of the large compressibility of the Cs coordination sphere.

The behaviour of the octahedra around the cations at the *B* sites in CsMgInF₆ reflects the mixed occupancies. Like in the InF₆ octahedra in Li₃Na₂In₂F₁₂ [11], the edge-length and angular distortions of the (In1/Mg1)F₆ and (In2/Mg2)F₆ octahedra increase on compression (Fig. 4). On the other hand, the shortest (In1/Mg1)–F and (In2/Mg2)–F interatomic distances (Table 3) compare well with the Mg–F distances in NaCaMg₂F₇ pyrochlore at high pressures [3].

The distortion of the high-pressure structure could be quantified by analysing its pseudosymmetry (program PSEUDO [12])⁴ with respect to space group *Imma* that is a minimal supergroup of *Pnma* (Figs. 1 and 5). The atomic displacements necessary to obtain a structure with symmetry *Imma* are below 0.15 Å for all atoms at ambient pressure [2]. They increase substantially on compression and are 0.322, 0.865, 1.273, 1.896, and 1.250 Å for the Cs, In2/Mg2, F1/F2, F3, and F4 atoms, respectively, at 6.04 GPa.⁵ It is noteworthy that these values are similar to the ones observed in other fluoride pyrochlores with symmetry *Pnma* ($Z = 4$) at ambient conditions, e.g., KCuAlF₆ (K: 0.184 Å, Cu: 0.823 Å, F1/F2: 1.216 Å, F3: 0.864 Å, F4: 0.898 Å, [13]).

Fig. 5 shows projections of selected defect pyrochlores with different degrees of distortions. As can be seen in Figs. 5a [13] and b [2], the distortions in CsMgInF₆ at ambient conditions with respect to the *Imma* structure are indeed minimal, with the six nearest fluorine atoms around the Cs¹⁺ cation at distances below 3.5 Å forming a slightly deformed octahedron. Ordered KCuAlF₆ [13] is significantly more deformed (Fig. 5c). It is remarkable that the coordination spheres around the Cs¹⁺ and the K¹⁺ cations in the structures of CsMgInF₆ at 6.04 GPa (Fig. 5d) and of KCuAlF₆ (Fig. 5c), respectively, include nine nearest fluorine neighbours below 3.5 Å. On the other hand, the deviation of the In2/Mg2 atoms from the position 0.25, 0.25, and 0.75 (the ideal position in *Imma*) is more pronounced in CsMgInF₆ than that of the corresponding atom in KCuAlF₆ so that the strong distortions of the (In2/Mg2)F₆ octahedra are noticeable. Figs. 5a–d clearly demonstrate that the effect of hydrostatic pressure on CsMgInF₆

is comparable to the effect of chemical pressure exerted through the incorporation of ions of different sizes into the *A* and *B* sites in AB²⁺B³⁺F₆ pyrochlores. The high-pressure structure of CsMgInF₆ also indicates that the degree of distortion of the pyrochlore structure can even be higher than what is observed in the related compounds at $P = 0.0001$ GPa. In this context it is interesting to consider the only monoclinic compound of the family, KCuCrF₆ (Fig. 5e, [14]). The structure of this material is very similar to the structure of KCuAlF₆, the main difference being a slightly larger inclination of the BF₆ octahedra with respect to the *c* axis and a more asymmetric coordination sphere around the K¹⁺ ion. It is thus remarkable that the pyrochlore structure, once it has reached a certain degree of deviation from the higher symmetric *Imma* structure, seems to follow two distinct paths to accommodate further distortions, one that is reflected in the high-pressure structure of disordered CsMgInF₆ and another that is occurring in ordered KCuCrF₆ at ambient pressure.

4. Conclusions

No ordering of the In³⁺ and Mg²⁺ cations is observed in CsMgInF₆ on compression to at least 6.94 GPa. The major contribution to the bulk compressibility arises from the changes in the coordination sphere around the Cs atoms. The effect of hydrostatic pressure on the crystal structure of CsMgInF₆ is comparable to the effect of chemical pressure owing to the incorporation of ions of different sizes into the *A* and *B* sites in defect AB²⁺B³⁺F₆ pyrochlores.

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Appendix A. Supplementary material

Supplementary data associated with this article can be found in the online version at 10.1016/j.jssc.2009.04.026.

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⁵ The displacement of the In1/Mg1 atoms is zero.